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**The Weak Axiom, the  $\sigma$ -Axiom  
and Complete Non-Transitive Rationality**

by

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# The Weak Axiom, the $\sigma$ -Axiom and Complete Non-transitive Rationality

Luigi Brighi\*

## 1 Introduction

This paper deals with the characterization of choices satisfying two kinds of behavioural axioms, the Weak Axiom of Revealed Preference (WA), introduced in demand theory by Samuelson (1938), and the  $\sigma$ -Axiom formulated by Clark (1988) in the abstract context of the theory of choice.

The WA is a mild requirement of consistency of choice. In consumer theory, for example, the WA does not imply the hypothesis of utility maximization since, as shown by Gale (1960), Shafer (1977), Peters and Wakker (1994) and John (1998), there are demand functions satisfying the WA that cannot be rationalized by transitive preferences. The  $\sigma$ -Axiom places more stringent restrictions on choice as compared to the WA, however, even the  $\sigma$ -Axiom is not strong enough to allow for a characterization in terms of complete and transitive preferences (as it will be the case for choice behaviour satisfying the Strong Axiom of Revealed Preference). In fact, in the special case of single-valued choice (e.g. demand functions), the two types of behavioural assumptions are equivalent.

This paper addresses the problem of finding the type of rationality corresponding to the  $\sigma$ -Axiom and the WA. It will be shown that the above type

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of choice behaviour can be rationalized by preferences which are complete and feature a certain ‘degree’ of transitivity.

The results are obtained within the abstract context of the theory of choice so that they also apply to the special but important case of demand theory. We provide stronger characterizations of the  $\sigma$ -Axiom and also stronger characterizations of the WA when choice is single-valued.

Section 2 contains notation and definitions. Section 3 reviews earlier characterizations of the WA. Section 4 presents some preliminary results and Section 5 provides new characterizations of the  $\sigma$ -Axiom and the WA.

## 2 Definitions

Let  $X$  be a set of alternatives and  $Q$  a binary relation in  $X$ , i.e.  $Q \subseteq X^2$ . If  $x \in X$  is related to  $y \in X$  we write  $(x, y) \in Q$  or, equivalently,  $xQy$ .

A strict preference  $Q$  is an irreflexive binary relation in  $X$ , i.e.  $Q \subseteq X^2$  and  $\neg xQx$  for all  $x$  in  $X$ . By  $Q(x)$  we denote the set of strictly preferred alternatives, i.e.  $Q(x) = \{z \in X \mid zQx\}$ , while  $Q^{-1}(x) = \{z \in X \mid xQz\}$  is the set of alternatives ‘dominated’ by  $x$ . The non-comparability relation  $I \subseteq X^2$  associated with  $Q$  is defined by  $xIy$  iff  $\neg xQy$  and  $\neg yQx$ . By  $Q^\alpha \subseteq X^2$  we denote the asymmetric component of  $Q$ , i.e.  $xQ^\alpha y$  iff  $xQy$  and  $\neg yQx$ . The symmetric component of  $Q$  is denoted by  $E$ , thus  $xEy$  iff  $xQy$  and  $yQx$ . Clearly,  $Q = Q^\alpha \cup E$ . A binary relation  $Q$  is asymmetric if  $xQy$  implies  $\neg yQx$ .

**Definition 1.** (SR and IR) The strict preference  $Q$  is

- i) *Superiorly Regular* (SR) if  $xIy$  implies  $Q(x) = Q(y)$  or, equivalently, if  $zQx$  and  $xIy$  imply  $zQy$ .
- ii) *Inferiorly Regular* (IR) if  $xIy$  implies  $Q^{-1}(x) = Q^{-1}(y)$  or, equivalently, if  $zIx$  and  $xQy$  imply  $zQy$ .

We notice that either SR or IR imply transitivity of the non comparability relation, i.e. if  $xIy$  and  $yIz$  then  $xIz$ . However, SR and IR do not imply transitivity of  $Q$ .

A non irreflexive binary relation  $R \subseteq X^2$  is a *weak* preference or, simply, a preference. A preference  $R$  is *reflexive* if  $xRx$  for all  $x \in X$ .  $R$  is *complete* if for all  $x, y \in X$  either  $xRy$  or  $yRx$  or both.

The asymmetric and the symmetric components of a preference  $R$  are respectively denoted by  $R^\alpha$  and  $R^\sigma$ , i.e.  $xR^\alpha y$  iff  $xRy$  and  $\neg yRx$ , and  $xR^\sigma y$  iff  $xRy$  and  $yRx$ . Clearly,  $R = R^\alpha \cup R^\sigma$ .

**Definition 2.** The preference  $R$  is

- i)  $\alpha\sigma$ -transitive if  $zR^\alpha x$  and  $xR^\sigma y$  imply  $zR^\alpha y$
- ii)  $\sigma\alpha$ -transitive if  $zR^\sigma x$  and  $xR^\alpha y$  imply  $zR^\sigma y$
- iii)  $\sigma\sigma$ -transitive if  $zR^\sigma x$  and  $xR^\sigma y$  imply  $zR^\sigma y$

$R$  is  $\sigma$ -transitive if i), ii) and iii) hold.

Notice that  $\sigma$ -transitivity does not imply transitivity of  $R$ .

Let  $\mathcal{A}$  be the set of all the subsets of  $X$  and  $\mathcal{B}$  any nonempty subset of  $\mathcal{A}$  which does not contain the empty set. A function  $\Phi: \mathcal{B} \rightarrow \mathcal{A}$  is a choice if  $\Phi(B) \subseteq B$  for all  $B \in \mathcal{B}$ .  $\Phi$  is decisive if  $\Phi(B) \neq \emptyset$  for all  $B \in \mathcal{B}$ .  $\Phi$  is single-valued if  $\Phi(B)$  is a singleton for all  $B \in \mathcal{B}$ .

A preference  $R$  rationalizes the choice function  $\Phi$  if for all  $B \in \mathcal{B}$

$$\Phi(B) = \{x \in B \mid xRy \text{ for all } y \in B\}.$$

$\Phi$  is rational if there exists some preference  $R$  satisfying the above condition.

A strict preference  $Q$  motivates the choice function  $\Phi$  if for all  $B \in \mathcal{B}$

$$\Phi(B) = \{x \in B \mid Q(x) \cap B = \emptyset\}.$$

$\Phi$  is motivated if there exists some strict preference  $Q$  satisfying the above condition.

To a choice function  $\Phi: \mathcal{B} \rightarrow \mathcal{A}$  is associated the *revealed preference*  $V \subseteq X^2$ , which is defined by  $xVy$  iff there exists  $B \in \mathcal{B}$  such that  $x \in \Phi(B)$  and  $y \in B$  (i.e.  $y$  is available when  $x$  is chosen). The revealed strict preference

$V^*$  is defined by  $xV^*y$  iff there exists  $B \in \mathcal{B}$  such that  $x \in \Phi(B)$  and  $y \in B - \Phi(B)$  (i.e.  $y$  is rejected when  $x$  is chosen).

**Definition 3.** The choice function  $\Phi: \mathcal{B} \rightarrow \mathcal{A}$  satisfies the Weak Axiom of Revealed Preference (WA) iff  $xV^*y$  implies  $\neg yVx$ .

### 3 Earlier characterizations

Clark (1988) and Scapparone (2000) provide some interesting results on the characterization of single valued choices satisfying the WA. Their results are brought together in the following

**Theorem 1.** Let  $\Phi$  be a single-valued choice. The following statements are equivalent:

- i)  $\Phi$  satisfies the WA
- ii)  $\Phi$  is rationalized by a  $\sigma$ -transitive preference  $R$
- iii)  $\Phi$  is motivated by a SR and IR strict preference  $Q$

*Proof.* (i) to (ii). It is well known that a choice satisfying the WA is rationalized by the revealed preference  $V$ . Moreover, since  $\Phi$  is single-valued  $V$  is antisymmetric, i.e.  $xVy$  and  $yVx$  imply  $x = y$ . Thus  $V^\sigma \subseteq \Delta = \{(x, y) \in X^2 \mid x = y\}$  and  $V$  is trivially  $\sigma$ -transitive. Hence  $R = V$  is  $\sigma$ -transitive and rationalizes  $\Phi$ .

(ii) to (iii). Set<sup>1</sup>  $Q = X^2 - R^{-1} - \Delta$ , i.e.  $xQy$  iff  $x \neq y$  and  $\neg yRx$ . Clearly,  $Q$  is irreflexive. Next, let us suppose that  $Q$  is not SR. Then, there exist  $x, y$  and  $z$  such that  $x \neq y$ ,  $xIy$ ,  $zQx$  and  $\neg zQy$ . By definition of  $Q$  we have  $xR^\sigma y$  and from  $xIy$  and  $zQx$  we have  $z \neq y$  so that  $\neg zQy$  yields  $yRz$ . From  $xR^\sigma y$  and  $yRz$  we obtain, by  $\sigma$ -transitivity,  $xRz$  which is impossible since  $zQx$  implies  $\neg xRz$ . Therefore,  $Q$  is SR. A similar argument shows that  $Q$  is also IR.

<sup>1</sup>Recall that  $R^{-1}$  denotes the inverse of the binary relation  $R$ , i.e.  $R^{-1} = \{(y, x) \in X^2 \mid (x, y) \in R\}$ .

Next, we show that  $Q$  motivates  $\Phi$ . It is easily seen that  $\Phi(B) \subseteq \Psi(B) = \{x \in B \mid Q(x) \cap B = \emptyset\}$  for all  $B \in \mathcal{B}$ . To show the converse let us suppose that  $x \in \Psi(B)$  and  $x \notin \Phi(B)$  for some  $B$ . By definition of  $\Psi$  we have  $\neg yQx$  for all  $y \in B$  and, for  $y \neq x$  we have  $xRy$ . Since  $x \notin \Phi(B)$  it must be  $\neg xRx$ . However, since  $R$  rationalizes  $\Phi$  and  $\Phi$  is decisive, there exists  $z \in \Phi(B)$ , hence  $zRx$ . On the other hand, since  $z \neq x$  and  $z \in B$  we also have  $xRz$ , thus  $zR^\sigma x$ . By  $\sigma$ -transitivity,  $xR^\sigma z$  and  $zR^\sigma x$  imply  $xRx$  and this contradiction establishes the result.

(iii) to (i). Let us suppose that  $\Phi$  violates the WA, i.e. there exist  $x$  and  $y$  such that  $xV^*y$  and  $yVx$ . Since  $Q$  motivates  $\Phi$  we have  $xIy$ . Moreover, since  $xV^*y$ , there exists a set  $B$  such that  $x, y$  and  $z \in B$ ,  $x \in \Phi(B)$  and  $zQy$ . Thus, by SR, we have  $zQx$  which is impossible since  $x$  is chosen in  $B$ .  $\square$

From the proof it can be noticed that (ii) and (iii) are sufficient conditions for the WA even when the choice function is not single-valued. Indeed, the assumption that  $\Phi$  is single-valued is only used in step (i) to (ii). However, a counter-example provided by Scapparone (2000) shows that the above characterization of the WA cannot be extended to the case of multi-valued choice functions. In fact, Clark (1988) has shown that for not necessarily single valued choices  $\sigma$ -transitivity characterizes a stronger behavioural axiom than the WA, precisely the  $\sigma$ -Axiom that will be discussed in Sec. 5

In the following section we derive a preliminary result which allows us to strengthen the existing characterizations of the  $\sigma$ -Axiom and the WA.

### 4 A preliminary result

Given a SR strict preference  $Q$  we propose a general method for constructing a subrelation  $P \subseteq Q$  which is asymmetric and preserves the SR property.

The construction of such a subrelation may seem a trivial matter. In fact, if we select ‘one half’ of  $E$ , i.e. an asymmetric set  $E^*$  such that  $E^* \cup E^{*-1} = E$ , we immediately obtain the asymmetric subrelation  $P = Q^\alpha \cup E^*$ . However,  $P$  need not preserve the SR property. For example, let  $X = \{x, y, z\}$  and  $Q =$

$\{(x, z), (z, x), (y, z), (z, y)\}$ . Then  $Q^\alpha = \emptyset$ ,  $E = Q$  and  $I = \{(x, y), (y, x)\}$ . Clearly,  $Q$  has the SR property and is not asymmetric. Let us consider the asymmetric set  $E^* = \{(x, z), (z, y)\}$ . Then  $E^* \cup E^{*-1} = E$  and the subrelation  $P = E^*$  is asymmetric. However,  $P$  has not the SR property since  $xIy$ ,  $z \in P(y)$  but  $z \notin P(x)$ .

In this trivial example it is easy to find a subrelation  $P$  which fulfill the desired requirements, e.g. set  $E^* = \{(z, x), (z, y)\}$ . In general, however, things are not so simple especially when the number of alternatives is not finite. Below we shall provide a general method for finding the desired subrelations.

For the rest of this section we assume that  $Q = Q^\alpha \cup E$  is a SR strict preference. Let us recall a few useful facts about the set  $E$ .

**Fact 1.**  $(z, y) \in E$  if and only if there exists  $(x, w) \in X^2$  such that  $(z, y)$  and  $(x, w)$  satisfy the following conditions:

$$\begin{aligned} &zQx, \quad xIy \\ &yQw, \quad wIz \end{aligned} \tag{1}$$

Indeed, (1) and SR imply  $(z, y) \in E$ . Conversely, (1) trivially holds for  $x = y$  and  $w = z$ .

**Fact 2.** If  $(z, y) \in E$  and  $(x, w) \in X^2$  satisfy (1) there are only three possible mutually exclusive cases:

- i)  $wQ^\alpha x$  iff  $zQ^\alpha x$
- ii)  $xQ^\alpha w$  iff  $yQ^\alpha w$
- iii)  $wEx$ .

*Proof.* Obviously, the three cases are mutually exclusive. To prove that they exhaust all the possibilities we must show that  $xIw$  is excluded. Indeed, by transitivity of  $I$ ,  $wIz$  would imply  $xIz$  which is impossible since  $zQx$ .

Next, let us consider the equivalence in (i) and suppose that  $xQz$ . Then from  $zIw$  and SR we have  $xQw$  which contradicts  $wQ^\alpha x$ , thus  $zQ^\alpha x$ . The converse and the equivalence in (ii) are proved in a similar way.  $\square$

**Fact 3.** If  $(z, y) \in E$  and  $(x, w), (x', w') \in X^2$  satisfy (1), then we cannot have  $zQ^\alpha x$  and  $yQ^\alpha w'$ . Indeed, in that case  $(z, y)$  and  $(x, w')$  would satisfy (1) which, by Fact 2, is impossible.

In order to construct the desired subrelation of  $Q$  we start the analysis from the following two subsets of  $E$ .

**Definition 4.** The sets  $E_1^* \subseteq E$  and  $E_2 \subseteq E$  are as follows:

$E_1^*$ :  $(z, y) \in E_1^*$  if for some  $(x, w) \in X^2$  satisfying (1) it holds  $zQ^\alpha x$ .

$E_2$ :  $(z, y) \in E_2$  if  $(z, y) \in E$  and for all  $(x, w) \in X^2$  satisfying (1) it holds  $xEw$ .

**Remark 1.** It is easily seen that the sets  $E_1^*$  and  $E_2$  are disjoint and that  $E_2$  is symmetric, i.e.  $(z, y) \in E_2$  implies  $(y, z) \in E_2$ . On the other hand, the set  $E_1^*$  is asymmetric. Indeed, if  $(z, y)$  and  $(y, z)$  were in  $E_1^*$  we would have the case excluded by Fact 3.

The next step consists in selecting an appropriate subset of  $E_2$ . To this aim we define a new family of subsets of  $E_2$ .

**Definition 5.** Let  $(z, y) \in E_2$ . The set  $G(z, y)$  consists of all  $(x, w) \in X^2$  satisfying (1).

A few useful properties of the sets  $G(z, y)$  are listed below.

**Lemma 1.** The set  $G(z, y)$  has the following properties:

- i)  $G(z, y) \neq \emptyset$  and  $G(z, y) \subseteq E_2$ .
- ii)  $G(z, y)$  is asymmetric.
- iii)  $G(y, z) = G(z, y)^{-1} := \{(w, x) \in X^2 \mid (x, w) \in G(z, y)\}$ .
- iv) If  $(x, w) \in G(z, y)$  then  $G(z, y) = G(z, x)$ .

The proof is the Appendix.

The sets  $G(z, y)$  allow us to obtain a partition of  $E_2$  by considering the following binary relation. For all  $(z, y)$  and  $(z', y')$  in  $E_2$ ,

$$(z, y) \mathcal{R} (z', y') \quad \text{iff} \quad G(z, y) = G(z', y')$$

It is easily seen that  $\mathcal{R}$  is an equivalence relation, i.e. it is reflexive, symmetric and transitive, therefore  $E_2$  can be partitioned into equivalence classes. We denote by  $\mathcal{C}$  the family of equivalence classes and by  $C$  a generic element of  $\mathcal{C}$ , thus  $E_2 = \cup_{C \in \mathcal{C}} C$  and  $C \cap C' = \emptyset$  for all  $C \neq C'$ .

**Lemma 2.** Let  $C \in \mathcal{C}$ . Then (i)  $C$  is asymmetric and (ii)  $C^{-1} \in \mathcal{C}$ .

The proof is in the Appendix.

**Definition 6.** Let  $E_2^* := \cup_{C \in \mathcal{D}} C$ , where  $\mathcal{D}$  is a subset of  $\mathcal{C}$  such that, for all  $C \in \mathcal{C}$  it holds either  $C \in \mathcal{D}$  or  $C^{-1} \in \mathcal{D}$  (but not both).

The existence of the set  $\mathcal{D}$  in the definition of  $E_2^*$  is guaranteed by the Axiom of Choice noticing that, by Lemma 2, the set  $\mathcal{C}$  can be partitioned by the family of sets  $\{C, C^{-1}\}$ .

**Remark 2.** The set  $E_2^*$  is asymmetric and  $E_2^* \cup E_2^{*-1} = E_2$ . The first claim follows trivially from Definition 6 and Lemma 2(i). As for the equality, the first inclusion is trivial. To show the converse, let  $(z, y) \in E_2$  so that  $(z, y) \in C$  for some  $C \in \mathcal{C}$ . If  $C \in \mathcal{D}$  then  $(z, y) \in E_2^*$ . If  $C \notin \mathcal{D}$  then  $C^{-1} \in \mathcal{D}$  and  $(y, z) \in E_2^*$  so that  $(z, y) \in E_2^{*-1}$ .

The final step of the construction is to set

$$E^* := E_1^* \cup E_2^*. \quad (2)$$

**Lemma 3.** The set  $E^*$  is asymmetric and  $E^* \cup E^{*-1} = E$ .

The proof is in the Appendix.

The main result of this section is the following

**Theorem 2.** Let  $\Phi$  be a decisive choice (not necessarily single-valued) motivated by a strict preference  $Q$  satisfying the SR property. Then  $\Phi$  is motivated by a strict preference  $P$  with the following properties:

- i)  $P$  is an asymmetric subrelation of  $Q$ , i.e.  $P$  is asymmetric and  $P \subseteq Q$ .
- ii)  $P$  has the same non comparability relation as  $Q$ , i.e.  $I = X^2 - Q \cup Q^{-1} = X^2 - P \cup P^{-1}$ .
- iii)  $P$  has the SR and IR properties.

*Proof.* Set  $P = Q^\alpha \cup E^*$  where  $E^*$  is given by (2). Then, by Lemma 3, it is easily seen that  $P$  satisfies (i) and (ii).

As for (iii), let us suppose that  $P$  does not satisfy the SR property, i.e. there exist  $x, y$  and  $z$  such that  $xIy, z \in P(x)$  and  $z \notin P(y)$ . Since  $Q$  is SR and  $z \in P(x) \subseteq Q(x)$  we have  $(z, y) \in Q$ . Thus, since  $(z, y) \notin P$  it must be  $(z, y) \in E$  and specifically  $(z, y) \in E^{*-1}$  or equivalently  $(y, z) \in E^*$ . We will show that this leads to a contradiction.

Let us suppose that  $(y, z) \in E_1^*$ , so that there exists  $w \in X$  such that  $yQ^\alpha w$  and  $wIz$ . Thus, we can write

$$\begin{aligned} &yQ^\alpha w, \quad wIz \\ &zQx, \quad xIy \end{aligned}$$

By Fact 2(ii) we have  $xQ^\alpha w$  and it is easily seen that  $(x, z) \in E_1^*$ . Thus  $x \in P(z)$ , which is impossible since  $z \in P(x)$  and  $P$  is asymmetric. Therefore, we conclude that  $(y, z) \notin E_1^*$ .

Next, let us suppose that  $(y, z) \in E_2^*$  so that  $(y, z)$  belongs to an equivalence class, i.e.  $(y, z) \in C$  for some  $C \in \mathcal{C}$ . Moreover, since  $(y, z) \in E_2$  and  $(z, x)$  satisfy (1), by Lemma A (in the Appendix), we also have  $(x, z) \in E_2$ . We show that  $(x, z) \in C$ , i.e.  $G(y, z) = G(x, z)$ .

By symmetry of  $E_2$ ,  $(y, z) \in E_2$  implies  $(z, y) \in E_2$ , thus there exists  $w \in X$  such that  $(x, w) \in G(z, y)$ . Then by Lemma 1(iv),  $G(z, y) = G(z, x)$ , so that  $G(z, y)^{-1} = G(z, x)^{-1}$  and by Lemma 1(iii)  $G(y, z) = G(x, z)$ . Since  $(y, z)$  and  $(x, z)$  belong to the same equivalence class  $C$  and  $(y, z) \in E_2^*$ , we also have  $(x, z) \in E_2^*$ . But that means  $x \in P(z)$ , which is impossible since  $P$  is asymmetric and  $z \in P(x)$  by assumption. Hence  $(y, z) \notin E_2^*$  and we conclude that  $P$  has the SR property. To complete point (iii) we show that an asymmetric and SR preference is also IR. Indeed, let us suppose that IR is violated, i.e. there exist  $xIy, xPz$  and  $\neg yPz$ . We have two cases: (a)  $zPy$ ,

then SR yields  $zPx$  which is impossible since  $P$  is asymmetric. (b)  $\neg zPy$ , so that  $zIy$  and since  $xPz$  SR yields  $xPy$  which is impossible since  $xIy$ . Thus we conclude that  $P$  is also IR.

Finally, we show that  $P$  motivates  $\Phi$ . Let  $\Psi(B) = \{x \in B; P(x) \cap B = \emptyset\}$ . Since  $\Phi$  is motivated by  $Q$  and  $P(x) \subseteq Q(x)$ , it is easily seen that  $\Phi(B) \subseteq \Psi(B)$ . To show the converse let  $x \in \Psi(B)$  so that  $P(x) \cap B = \emptyset$ . Arguing by contradiction, let us suppose that  $x \notin \Phi(B)$ , which means that there exists  $z$  such that  $z \in Q(x) \cap B$ . Since  $\Phi$  is decisive there exists  $y \neq x$  such that  $y \in \Phi(B)$ , thus  $y \in \Psi(B)$  since  $P(x) \subseteq Q(x)$ . Clearly,  $x$  and  $y$  are non comparable under  $P$  and, by (ii), also under  $Q$ , i.e.  $xIy$ . However, since  $Q$  has the SR property and  $zQx$ , it must be  $zQy$  so that  $z \in Q(y) \cap B$  and  $y$  cannot be in  $\Phi(B)$ . Therefore, we conclude that  $P$  motivates  $\Phi$ .

□

## 5 Characterizations by means of complete or asymmetric preferences

As we noticed in Sec. 3, Theorem 1 cannot be extended to the case of multivalued choices. In fact, as shown by Clark (1987),  $\sigma$ -transitive preferences characterize choices satisfying a stronger property than the WA. In order to introduce this new behavioural axiom let us recall a few definitions. The composition of two relations  $S$  and  $T$ , denoted by  $S \circ T$ , is defined by  $x(S \circ T)y$  iff there exists  $z$  such that  $xSz$  and  $zTy$ . The transitive closure of  $S$ , denoted by  $S^\tau$ , is the smallest transitive relation containing  $S$ .

**Definition 7.** The choice function  $\Phi$  satisfies the  $\sigma$ -Axiom iff the relation  $V^* \circ (V^\sigma)^\tau$  is asymmetric.

It is easily seen that a choice satisfying the  $\sigma$ -Axiom obeys the WA.<sup>2</sup> The converse, however, is not generally true so that the  $\sigma$ -Axiom is stronger than

<sup>2</sup>Let us suppose that the WA does not hold, i.e. there are  $x$  and  $y$  such that  $xV^*y$  and  $yVx$ . Then  $xV^\sigma y$  and  $x(V^* \circ (V^\sigma)^\tau)x$  so that the  $\sigma$ -axiom is violated.

the WA. Clark [(1987), Corollary (VI)] shows that the  $\sigma$ -Axiom is characterized by  $\sigma$ -transitive rationality. The following theorem provides a stronger characterization.

**Theorem 3.** Let  $\Phi$  be a decisive choice (not necessarily single-valued). The following statements are equivalent:

- i)  $\Phi$  satisfies the  $\sigma$ -Axiom
- ii)  $\Phi$  is rationalized by a  $\sigma$ -transitive preference
- iii)  $\Phi$  is motivated by a SR and IR strict preference
- iv)  $\Phi$  is motivated by an asymmetric SR and IR preference
- v)  $\Phi$  is rationalized by a complete and  $\sigma$ -transitive preference

*Proof.* (i) and (ii) are equivalent by Corollary (VI) in Clark (1987). (ii) implies (iii) as it is shown in (ii) to (iii) of Theorem 1. (iii) implies (iv) by Theorem 2. To show that (iv) implies (v) let  $P$  be asymmetric, IR, SR and motivate  $\Phi$ , then set  $R = X^2 - P^{-1}$ . It is easily seen that  $R$  is complete and rationalizes  $\Phi$ . Moreover,  $R^\alpha = P$  and  $R^\sigma = I$  therefore, SR and IR imply  $\sigma$ -transitivity of  $R$ . Finally, (v) trivially implies (ii). □

When the choice is single-valued, the WA is equivalent to the  $\sigma$ -Axiom. Indeed, the WA is equivalent to  $V^* = V^\alpha$  and, when  $\Phi$  is single-valued, it implies that  $V$  is antisymmetric, thus  $V^\sigma \subseteq \Delta = \{(x, y) \mid x = y\}$ . Hence  $V^* \circ (V^\sigma)^\tau = V^* \circ V^\sigma \subseteq V^* = V^\alpha$  and the  $\sigma$ -Axiom holds.

Therefore, we obtain as a corollary of Theorem 3 the following characterization of the WA which improves upon Theorem 1.

**Corollary.** Let  $\Phi$  be a single-valued choice. The following statements are equivalent:

- i)  $\Phi$  satisfies the WA
- ii)  $\Phi$  is motivated by an asymmetric SR and IR preference
- iii)  $\Phi$  is rationalized by a complete and  $\sigma$ -transitive preference

The Corollary directly applies to the case of demand functions and can be compared to a result by Kim and Richter [1986, Th. 16] according to which the WA is characterized by complete and convex preferences. As a final remark we notice that both the characterizations of demand functions offered by the Corollary and Theorem 16 in Kim and Richter (1986) are not completely satisfactory, since the characterizing preferences do not ensure the existence of a demand function, i.e. there may not exist a best bundle in each budget set. It is an open question whether a more satisfactory subclass of complete and  $\sigma$ -transitive preferences can be found.

## Appendix

**Lemma A.** If  $(z, y) \in E_2$  and  $(x, w)$  satisfies (1) then  $(x, w)$ ,  $(z, x)$  and  $(y, w)$  are in  $E_2$ .

*Proof.* Let us first show that  $(z, x) \in E_2$ . By (1) we have  $zQx$  and by  $(z, y) \in E_2$  we have  $xEw$ . Thus, by SR,  $xQw$  and  $wIz$  yield  $xQz$ . Thus  $(z, x)$  is in  $E$ .

Let  $(z, x)$  and  $(x', w') \in X^2$  satisfy conditions (1), i.e.

$$\begin{aligned} zQx', & \quad x'Ix \\ xQw', & \quad w'Iz \end{aligned}$$

If  $w'Q^\alpha x'$  then, by Fact 2,  $zQ^\alpha x'$ . Noting that, by SR,  $x'Ix$  and  $xIy$  yield  $x'Iy$  we see that  $(z, y)$  and  $(x', w)$  satisfy (1) so that  $(z, y) \in E_1^*$  which contradicts  $(z, y) \in E_2$ .

Next, let us suppose that  $x'Q^\alpha w'$ . Then, by Fact 2,  $xQ^\alpha w'$  and it is easily seen that  $(x, z)$  and  $(w', y)$  satisfy (1). By Fact 2 and  $xQ^\alpha w'$  we then have  $yQ^\alpha w'$ , therefore  $(y, z)$  and  $(w', x)$  satisfy (1) and  $(y, z) \in E_1^*$ . But this contradicts  $(z, y) \in E_2$  since  $E_2$  is symmetric and  $E_1^*$  and  $E_2$  are disjoint.

Thus, by Fact 2, we conclude that for all  $(x', w')$  it must be  $x'Ew'$  so that  $(z, x) \in E_2$ .

The remaining two cases are shown similarly. For example, notice that  $(x, z) \in E_2$  and  $(w, y)$  satisfy (1) so that, as shown above,  $(x, w) \in E_2$ .  $\square$

### Proof of Lemma 1.

(i) It is easily verified that  $(y, z) \in G(z, y)$ . Next,  $(x, w) \in G(z, y)$  implies, by Lemma A, that  $(x, w) \in E_2$ .

(ii) Let  $(x, w) \in G(z, y)$  then, by Definition 5,  $wIz$ . If  $(w, x)$  is in  $G(z, y)$  then  $zQw$  which contradicts  $wIz$ .

(iii) We have to show that  $(x, w) \in G(z, y)$  iff  $(w, x) \in G(y, z)$ . This follows trivially from (1).

(iv) By Lemma A,  $(z, x) \in E_2$  thus  $G(z, x)$  is well defined. First, we show that  $G(z, y) \subseteq G(z, x)$ .

Let  $(x', w') \in G(z, y)$ , i.e.  $(z, y)$  and  $(x', w')$  satisfy conditions (1) so that we have  $zQx'$ . Moreover,  $x'Ix$  follows from SR,  $x'Iy$  and  $yIx$ . Next, it is easily seen that  $(z, y)$  and  $(x', w')$  satisfy (1), therefore we have  $w'Iz$  and, by Lemma A,  $xQw'$ . Hence  $(z, x)$  and  $(x', w')$  satisfy (1) and we conclude that  $(x', w') \in G(z, x)$ .

The inclusion  $G(z, x) \subseteq G(z, y)$  is shown in a similar way.  $\square$

### Proof of Lemma 2.

(i) If  $(z, y)$  and  $(y, z)$  are in the same equivalence class we have  $G(z, y) = G(y, z)$ . Then, by Lemma 1(iii),  $G(z, y) = G(z, y)^{-1}$ , which is impossible since  $G(z, y)$  is asymmetric and non empty.

(ii) Let  $(z, y) \in C$ . By (i),  $C$  is asymmetric thus  $(y, z) \notin C$ . Therefore  $(y, z) \in C'$  for some  $C' \in \mathcal{C}$  with  $C' \neq C$ . We have to show that  $C' = C^{-1}$ . Now, let  $(y', z') \in C'$ . Thus  $G(y, z) = G(y', z')$  so that  $G(y, z)^{-1} = G(y', z')^{-1}$  and, by Lemma 1(iii),  $G(z, y) = G(z', y')$ . Hence  $(z', y') \in C$  and  $(y', z') \in C^{-1}$ . Therefore, we have shown that  $C' \subseteq C^{-1}$ . The converse is also true and is proved similarly.  $\square$

### Proof of Lemma 3.

Let  $(z, y) \in E^*$  and  $(y, z) \in E^*$ . By Remark 1 and 2  $E_1^*$  and  $E_2^*$  are asymmetric thus  $(z, y) \in E_1^*$  and  $(y, z) \in E_2^*$  (or vice versa). Since  $(y, z) \in E_2^*$  we also have  $(z, y) \in E_2$ , which is impossible since  $E_1^*$  and  $E_2$  are disjoint.

Next, we show that  $E \subseteq E^* \cup E^{*-1}$ . Let  $(z, y) \in E$ , then by Fact 1, 2 and 3 we have the following cases:

(a) For some  $(x, w) \in X^2$  satisfying (1) it holds  $xQ^\alpha w$ . Then, by Definition 4,  $(z, y) \in E_1^* \subseteq E^* \cup E^{*-1}$ .

(b) For some  $(x, w) \in X^2$  satisfying (1) it holds  $wQ^\alpha x$ . Then, by Definition 4,  $(y, z) \in E_1^*$  thus  $(z, y) \in E_1^{*-1} \subseteq E^* \cup E^{*-1}$ .

(c) Finally, for all  $(x, w) \in X^2$  satisfying (1) it holds  $xEw$ . Then, by Definition 4,  $(z, y) \in E_2$  and, by Remark 3,  $E_2 \subseteq E^* \cup E^{*-1}$ .

This completes the proof, since the inclusion  $E^* \cup E^{*-1} \subseteq E$  trivially holds.  $\square$

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